



## 1 SUMMARY

Calculates the coefficients of the **piece-wise cubic** function which **interpolates**  $n$  **given function values**  $f_i$  at points  $x_i, i=1, 2, \dots, n$ .

The interpolation function derived will be continuous and have continuous first derivatives. If the function values lie on a quadratic polynomial, this will be represented exactly. The subroutine returns the coefficients of the  $n-1$  cubics  $C_i(\theta)$  corresponding to the  $n-1$  intervals  $x_i$  to  $x_{i+1}$  in the transformed variables

$$\theta = \frac{x - x_i}{x_{i+1} - x_i}, \quad \text{i.e.} \quad C_i(\theta) = a_1 + a_2\theta + a_3\theta^2 + a_4\theta^3 \quad 0 \leq \theta \leq 1$$

**ATTRIBUTES** — **Version:** 1.0.0. **Types:** TB03A; TB03AD. **Original date:** July 1964. **Origin:** D.Miller, Harwell.

## 2 HOW TO USE THE PACKAGE

### 2.1 Argument list

*The single precision version*

CALL TB03A(N, F, X, A)

*The double precision version*

CALL TB03AD(N, F, X, A)

**N** is an **INTEGER** variable which must be set by the user to  $n$ , the number of function values passed in the array **F**. **N** is not altered by the subroutine. **Restriction:**  $n \geq 4$ .

**F** is a **REAL** (**DOUBLE PRECISION** in the **D** version) array which must be set by the user to contain the function values  $f_i, i=1, 2, \dots, n$ . **F** is not altered by the subroutine.

**X** is a **REAL** (**DOUBLE PRECISION** in the **D** version) array which must be set by the user to contain the values of the points  $x_i, i=1, 2, \dots, n$ . **X** is not altered by the subroutine. **Restriction:** the points must be ordered and distinct, i.e.  $x_1 < x_2 < \dots < x_n$ .

**A** is a two-dimensional **REAL** (**DOUBLE PRECISION** in the **D** version) array of first dimension 4 and second dimension at least  $n-1$ , which is set by the subroutine to the coefficients of the cubics for the  $n-1$  intervals. In the interval  $x_i$  to  $x_{i+1}$  the function is represented by the cubic

$$C_i(\theta) = a_{1,i} + a_{2,i}\theta + a_{3,i}\theta^2 + a_{4,i}\theta^3$$

which is a good approximation to  $f\{(1-\theta)x_i + \theta x_{i+1}\}$ . The values of  $a_{j,i}, j=1, 2, 3, 4$  and  $i=1, 2, \dots, n-1$  are returned in **A**(**J, I**), **J**=1, 4 and **I**=1,  $n-1$ .

Note that the values of  $f_i$  and  $f_{i+1}$  are given by substituting  $\theta=0$  and  $\theta=1$  respectively, and values for  $x$  between  $x_i$  and  $x_{i+1}$  are given by values of  $\theta$  between 0 and 1.

**3 GENERAL INFORMATION**

**Use of common:** None.

**Workspace:** None.

**Other routines called directly:** None.

**Input/output:** None.

**Restrictions:** None.