PACKAGE SPECIFICATION

HSL ARCHIVE

1 SUMMARY

To compute values of the **Bessel functions** $I_1(x)$ and $K_1(x)$. A Chebyshev series in x is used if $0 \le x \le 8$ and a similar series in $\frac{1}{x}$ if x > 8, see, C.W. Clenshaw, 'Mathematical Tables', Vol. 5, NPL.

ATTRIBUTES — **Version:** 1.0.0. **Types:** FF04A; FF04AD. **Calls:** FD05. **Original date:** December 1966. **Origin:** S.Marlow, Harwell.

2 HOW TO USE THE PACKAGE

The single precision version

CALL FF04A(VI1,VK1,X,N)

The double precision version

CALL FF04AD(VI1,VK1,X,N)

- VII is a REAL (DOUBLE PRECISION in the D version) variable which is set by the subroutine to the computed value of $I_1(x)$.
- VK1 is a REAL (DOUBLE PRECISION in the D version) variable which is set by the subroutine to the computed value of $K_1(x)$.
- is a REAL (DOUBLE PRECISION in the D version) variable which must be set by the user to the value of the argument x. **Restriction:** $x \ge 0$; and $x \ne 0$, for a value of $K_1(x)$. Note: if x < 0 then |x| is used.
- N is an INTEGER variable which must be set by the user to select $I_1(x)$ or $K_1(x)$, or both, i.e. the allowed values of N are
 - 0 only $I_1(x)$ is calculated.
 - 1 only $K_1(x)$ is calculated.
 - 2 both $I_1(x)$ and $K_1(x)$ are calculated.

3 GENERAL INFORMATION

Use of common: none.

Workspace: none.

Other subroutines: none.

Input/Output: none.

Restrictions:

 $x \ge 0$ for $I_1(x)$,

x > 0 for $K_1(x)$.

Accuracies:

6 sig. figs using 4-byte arithmetic

9 sig. figs using 8-byte arithmetic.

FF04 HSL ARCHIVE

4 METHOD

A Chebyshev series in x is used if $0 \le x \le 8$ and a similar series in $\frac{1}{x}$ if x > 8, see, C.W. Clenshaw, 'Mathematical Tables', Vol. 5, NPL.